Title.

MASS ABSORPTION CORRECTIONS FOR BETA COUNTING OF 147ND AND 147PM AND THE DETERMINATION OF K(147PM)/(K(147ND)

Author(s):

Timothy Benjamin, C-INC Scott Bowen, C-INC

Submitted to:

AFTAC September 2002





Los Alamos National Laboratory, an affirmative action/equal opportunity employer, is described by the University of California for the U.S. Department of Energy under contract W-7405-ENG-36. By acceptance of this article, the publisher recognizes that the U.S. Government retains a nonexclusive, royalty-free license to publish or reproduce the published form of this contribution, or to allow others to do so, for U.S. Government purposes. Los Alamos National Laboratory requests that the publisher identify this article as work performed under the auspices of the U.S. Department of Energy. Los Alamos National Laboratory strongly supports academic freedom and a researcher's right to publish; as an institution, however, the Laboratory does not endorse the viewpoint of a publication or guarantee its technical correctness.

Mass Absorption Corrections for β Counting of ¹⁴⁷Nd and ¹⁴⁷Pm and the Determination of K(¹⁴⁷Pm)/K(¹⁴⁷Nd)

Scott Bowen and Tim Benjamin 9/5/02

¹⁴⁷Nd is one of the primary fission products used in weapons radiochemical diagnostics to determine the fission efficiency of a nuclear test. Its 11-day half-life is very convenient for measurements of samples containing recently produced fission products. However, for samples more than approximately four months old, ¹⁴⁷Nd will have almost entirely died away. Fortunately, the beta-decay daughter of ¹⁴⁷Nd, ¹⁴⁷Pm, has a half-life of 2.6 years. Although ¹⁴⁷Nd can be readily gamma counted, a beta-decay based calibration has been maintained to ensure the best possible sensitivity on low-activity samples. A new calibration would add ¹⁴⁷Pm in order to extend the fission product measurements out to samples up to 25 years old.

¹⁴⁷Pm calibrations are complicated by several factors including: 1) poor gamma-counting rates, 2) beta-counting interference by ¹⁴⁷Nd during the first several months after a calibration irradiation, 3) lack of a stable Pm carrier for a radiochemically separated sample, and 4) the need for a mass absorption function for the relatively low endpoint beta energy (225KeV, average energy about 60KeV). All of these aspects can be overcome using data collected by S. Bowen as reported in a memo on 2/28/92 (see attachment 1).

Part I

¹⁴⁷Nd and ¹⁴⁷Pm Mass Absorption Corrections

The samples were prepared from aliquots of a stock solution consisting of the Nd fractions from several event 1152 'A' solutions with the addition of four different quantities of Nd carrier. The evolution of the parent-daughter, ¹⁴⁷Nd/¹⁴⁷Pm, pair was followed for three to four months using Counter 25, shelf one, followed by another month of counting on Counter 14 in three different geometries. The principle difference between these two beta counters is the Compton-suppressed background of Counter 25. (Due to the high early count rates, it would have been better to use Counter 14 initially and then Counter 25 for the lower activity of the predominately ¹⁴⁷Pm daughter. Even better would have been to leave the samples on a single counter throughout.)

S. Bowen originally assessed the data with the codes 'CPM' and 'CLSQ' in his 1992 memo. The current evaluation uses a fully-weighted linear-least-squares code, 'Winfit', written by C. Duffy for the weapons radiochemistry program. The activity data from multi-component systems is linearized (see attachment 2). The background data for each sample is tested for outliers using Chauvenet's Criterion and the average value is applied to each measurement. The <u>statistical</u> uncertainties are compounded in the usual RMS (root-mean-square) manner and co-variances are included where necessary. In this instance, the slope of the regression line is a measure of the activity (cpm) of the ¹⁴⁷Nd at

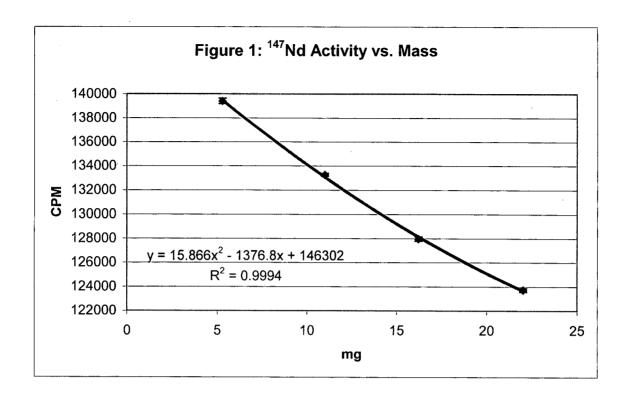
separation time (Table 1). The intercept contains information related to the ingrowth of the daughter ¹⁴⁷Pm as well as containing any ¹⁴⁷Pm that carried through the column separation. From these two values it is possible to calculate the <u>relative</u> counting efficiencies of these nuclides (Table 1). If the chemical separation is quantitative, then this efficiency ratio can be employed to characterize the relative count rate of the daughter ¹⁴⁷Pm in these samples.

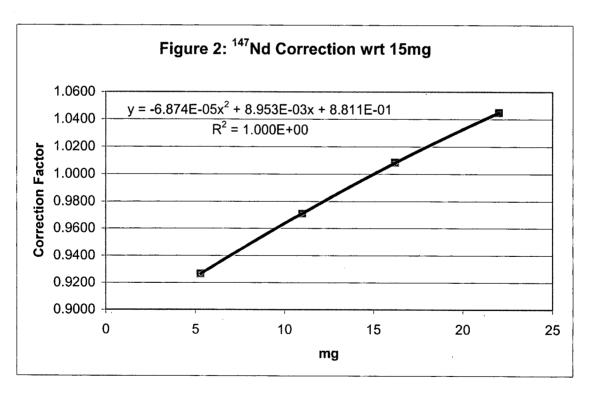
Table 1

Sample	Counter	Shelf	20 mg Absorber	Mass (mg)	¹⁴⁷ Nd cpm T _{sep}	sigma %	$\epsilon^{147} Pm/\epsilon^{147} Nd$	sigma %
5	25	1	No ·	5.284	1.394E+05	0.16%	0.208	0.86%
10	25	1	No	11.006	1.333E+05	0.10%	0.178	0.36%
15	25	1	No	16.211	1.280E+05	0.15%	0.161	1.0%
20	25	1	No	22.024	1.237E+05	0.12%	0.142	0.51%
10	14	1	No	11.006	1.292E+05	3.4%	0.178	4.2%
20	14	1	No	22.024	1.335E+05	4.1%	0.130	5.5%
5	14	2	No	5.284	8.248E+04	0.71%	0.224	0.98%
15	14	2	No	16.211	8.421E+04	0.59%	0.162	0.90%
5	14	2	Yes	5.284	4.790E+04	0.66%	0.0188	3.6%
15	14	2	Yes	16.211	4.921E+04	0.68%	0.0149	4.6%

The relative trends of 147 Nd cpm and ϵ^{147} Pm/ ϵ^{147} Nd are consistent with expectations for the Counter 25 data. However, the 147 Nd cpm trends for the Counter 14 data is uniformly in the opposite direction. In all three geometries the heavier sample is higher by 2 to 3%. As these are the same samples as counted on Counter 25 and the efficiency ratios are all consistent with proper sample identification on Counter 14, a plausible cause of the count rate discrepancy is presented below in Part II. Only the Counter 25 data is used for the purpose of establishing 147 Nd and 147 Pm mass absorption curves.

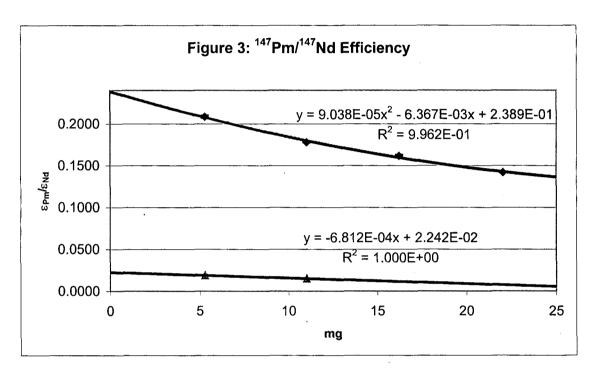
Figure 1 contains the 147 Nd cpm data (with plotted 1σ uncertainties) vs. the weight of the sample (mg). Note that the error bars are of the same size as the plotted symbols. As the uncertainties are approximately equal, an unweighted Excel regression line is adequate. A quadratic function is used to model the expect curvature. This curvature is the result of the differential absorption of the two principle β^- decay energies of 147 Nd (15% at 370 KeV and 85% at 810 KeV). When this regression function is normalized to 15 mg (nominal 75% chemical yield on 20 mg of carrier) the mass absorption correction curve (Figure 2) results. Although the curvature of the quadratic in Figure 2 is small, it is the natural effect of the curvature shown in Figure 1.





The calculated efficiency ratios as a function of mass are shown in Figure 3. These efficiency ratios were derived from the regressions of the counting data and are not a further application of the results shown in Figures 1 and 2. The error bars are again comparable to the size of the plotted symbols. The upper line is for the Counter 25 data, the lower line is for the Counter 14, Shelf 2, with the 20 mg absorber. The Counter 14

data for the geometries without the absorber are more uncertain and show some scatter but are consistent with the Counter 25 based line. Since incomplete separation of Pm from Nd would not be expected to be reproducible and therefore would introduce scatter into the efficiency ratio calculation, the tight array in Figure 3 is supportive of a clean separation. As expected, due to the different β energies of the two nuclides, slight curvature is observed in the data. The Counter 14 data with the absorber is underdetermined with respect to a quadratic fit; however, the absorber's suppression of both the ¹⁴⁷Pm and lower energy ¹⁴⁷Nd β swould naturally result is less curvature than that observed for Counter 25 without the absorber.



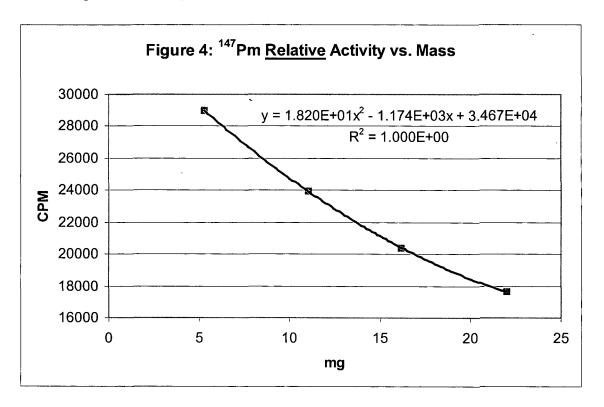
From the efficiency ratios and the deduced 147 Nd initial activities at separation time, the mass absorption curve for 147 Pm can be obtained. Multiplying the 147 Nd count rate by the 147 Pm/ 147 Nd efficiency ratio yields the relative 147 Pm count rate as a function of mass (Figure 4). In this instance, the curvature is due to the thicker samples beginning to approach infinite thickness for 147 Pm β -'s. The shape of this curve should then be essentially 1/x. These results can then be used to construct the 147 Pm mass absorption curves (Figure 5) by simply normalizing to the nominal 15 mg value. As would be expected, the normalized data (the reciprocal of 1/x) show a linear correction. The low β - energy results in a marked effect of nearly 3% per mg.

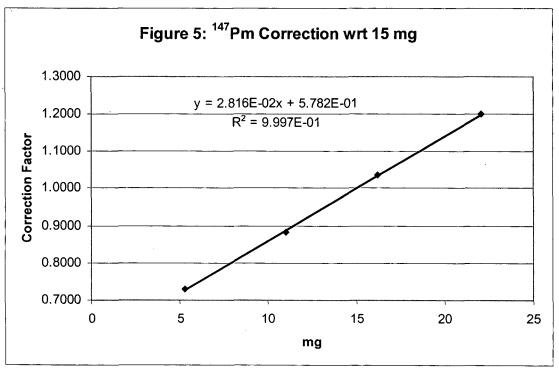
The final results are the two mass absorption correction functions for ¹⁴⁷Nd and ¹⁴⁷Pm. The uncertainties in the application of these correction factors is likely to be better than 1%, based on the quality of the data presented in these figures.

 $^{^{147}}$ Nd correction factor = 0.8811 + 8.953E-3 x_{mg} - 6.874E-5 x_{mg}^{2}

 $^{^{147}}$ Pm correction factor = 0.5782 + 2.816E-2 x_{mg}

(Note that the ¹⁴⁷Nd correction presented by S. Bowen in 1992 averages only 0.4% higher than these presented here.)





The ¹⁴⁷Pm/¹⁴⁷Nd K-Factor Ratio

The efficiency ratio relationship presented above can be used to calculate K-factor ratio for parent-daughter pairs like ¹⁴⁷Nd-¹⁴⁷Pm where the daughter's half-life is longer than the parent's. In this instance, the application would be converting the measured ¹⁴⁷Pm activity data to <u>exactly</u> the number of fissions that would have been measured at an earlier time by ¹⁴⁷Nd. Again, the uncertainties should be less than 1%.

$$K(^{147}Pm)/K(^{147}Nd) = {(\lambda_{Nd} - \lambda_{Pm})/\lambda_{Pm}}/{\{\epsilon_{Pm}/\epsilon_{Nd}\}}$$

For the 15 mg reference mass,

$$K(^{147}Pm)/K(^{147}Nd) = 527$$
 (for Counter 25, Shelf 1, No Absorber)

$$K(^{147}Pm)/K(^{147}Nd) = 7070$$
 (for Counter 14, Shelf 2, 20 mg/cm² Absorber)

Part II

The Apparent Counter 14 Anomaly

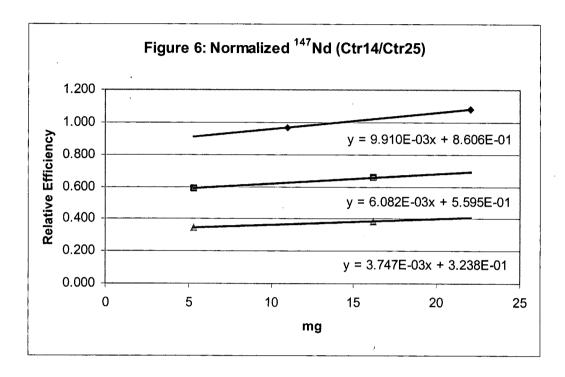
The observed increases in the calculated ¹⁴⁷Nd T_{sep} count rates for the heavier samples suggested a possible connection with the carrier itself (R. Gritzo, pers. comm.). The activity data from Table 1 is normalized to the corresponding Counter 25 data and presented in Table 2. (Note that the Counter 25 data is dominated by the actual decay of ¹⁴⁷Nd whereas the Counter 14 data is predominately ¹⁴⁷Pm daughter, which is used to calculate the equivalent ¹⁴⁷Nd parent, needed to support this activity.) Figure 6 is constructed from this Table. The linear fits indicate the relative efficiencies of the Counter 14 geometries. When the zero-mass (intercept) values are used to renormalized the data in Table 2, all the data is then on the same scale (intercept values becoming unity) (Figure 7). It is apparent that all three geometries show the same rate of increase with respect to carrier mass, 1.14% / mg.

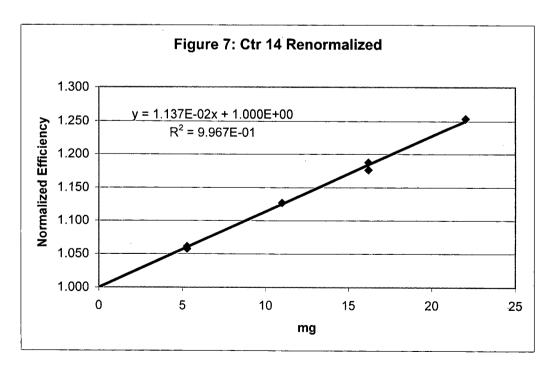
Table 2

mg	Ctr14-1/Ctr25	Ctr14-2/Ctr25	Ctr14-2Abs/Ctr25
5.284		0.592	0.344
11.006	0.970		
16.211		0.658	0.385
22.024	1.079		

This is consistent with a model of a very minor contamination in the Nd carrier at this time. Based on the last counts of the samples on Counter 14, shelf 2, with absorber, the apparent contaminant amounts to 0.20 cpm/mg. From the Figure 6 relative efficiencies,

the count rate for the other two geometries would be 0.35 cpm/mg (Counter 14, shelf 2, without absorber) and 0.53 cpm/mg (Counter 14, shelf 1, without absorber). These count rates are too small to affect the high-activity ¹⁴⁷Nd results from Counter 25. These data demonstrated that low count rate samples are sensitive to very small sources of contamination.





Promethium-147 Experiment

02/28/92

1) The following tube numbers from the Ln HPLC run on shot 1152 were combined in a 50 mL Erlenmeyer flask:

Jug Number	<u>Tubes</u>
2	195-205
3	194-204
4	196-205
5	195-204
6	197-204

- 2) The sample was boiled to dryness and heated at 600 °C for approximately one hour.
- 3) The sample was dissolved in concentrated HCl, a mixture of HNO₃ and HCLO₄ was added, and the sample was fumed to near dryness.
- 4) The sample was transferred to a 500 mL volumetric flask with $3\underline{M}$ HCl and the volume brought up to 500 mL with 3 \underline{M} HCl. This was the stock solution.
- 5) 1, 3, and 5 mL fractions of the stock were removed and placed in plastic scintillation vials. All volumes were brought up to 5 mL with H₂O and counted on Ge(Li) counter 76, shelf 10. RAYGUN analysis of the three samples for 147 Nd atoms at 308.542,1991 (the estimated Nd-Pm separation time for the columns) per mL of solution gave values of 9.125E9 \pm 0.6%, 9.190E9 \pm 0.5%, and 9.212E9 \pm 0.6%, respectively.
- 6) Four 1 mL fractions of the stock solution were removed and placed in centrifuge cones with 0.5, 1.0, 1.5, and 2.0 mL of standardized Nd carrier (11.42 mg Nd₂O₃ per mL). The oxides were precipitated with NH₄OH, fired at 1100 °C

for 30 minutes, weighed, and mounted on Al counting cards in the standard lanthanide oxide mounting geometry.

ML added	Ppt weight	Chem yield
0.5	5.284 mg	0.9254
1.0	11.006 mg	0.9638
1.5	16.211 mg	0.9464
2.0	22.024 mg	0.9643

7) The mounted samples were first counted on Ge(Li) counter 72, shelf 10 to measure ¹⁴⁷Nd atoms at 308.542,1991. This gave the following results:

Ppt weight	Atoms at T/mL
5.284 mg	9.073E9±0.64%
11.006 mg	9.326E9±0.82%
16.211 mg	9.164E9±0.70%
22.024 mg	9.324E9±0.61%

8) The samples were next counted on beta counter 25, shelf 1 (no absorber). The CPM program was run on the data from these samples using 2 components (147 Pm, $t_{1/2} = 2.623$ years and 147 Nd, $t_{1/2} = 10.990$ days). The CLSQ program was also run. The following 147 Nd values were obtained:

Weight	Cpm at T	<u>Err</u>	Cpm at T	<u>Err</u>
<u>(mg)</u>	(CPM)	<u>%</u>	(CLSQ)	<u>%</u>
5.284	1.377E5	0.1	1.377E5	1.5
11.006	1.315E5	0.1	1.314E5	1.0
16.211	1.264E5	0.1	1.262E5	1.5
22.024	1.221E5	0.1	1.219E5	0.9

These values are plotted on the attached plot. The y-intercept, 1.422E5, is the extrapolated no mass absorption cpm value. A plot of measured cpm divided by 1.422E5 versus sample mass gives a mass absorption correction curve. This is also attached.

Attachment 1

The corresponding ¹⁴⁷Pm values obtained from these beta analyses were:

<u>Weight</u>	Cpm at T	<u>Err</u>	Cpm at T	<u>Err</u>
<u>(mg)</u>	<u>(CPM)</u>	<u>%</u>	(CLSQ)	<u>%</u>
5.284	3.302E2	0.7	3.296E2	4.8
11.006	2.709E2	0.3	2.682E2	1.6
16.211	2.339E2	0.9	2.348E2	6.1
22.024	2.012E2	0.3	2.015E2	1.8

These samples were also counted on beta counter 14 with some of the samples counted through a 20 mg absorber to reduce the ¹⁴⁷Pm beta contribution. The data for counts with the absorber present were analyzed by assuming either a one or two component system.

The Nd results were:

<u>Weight</u>	<u>Absorber</u>	Cpm at T	<u>Err</u>	Cpm at T	<u>Err</u>
<u>(mg)</u>		<u>(CPM)</u>	<u>%</u>	(CLSQ)	<u>%</u>
5.284	No	8.177E4	0.6	8.126E4	2.0
5.284	Yes	5.389E4	0.8	5.798E4	0.4
5.284*	Yes	4.492E4	3.0	4.759E4	0.8
11.006	No	1.266E5	5.0	1.445E5	12.8
16.211	No	8.291E4	0.6	8.302E4	1.6
16.211	Yes	5.794E4	0.9	5.713E4	0.4
16.211*	Yes	4.995E4	1.3	4.897E4	0.8
22.024	No	1.296E5	5.6	1.463E5	10.1

^{*} Two component calculation

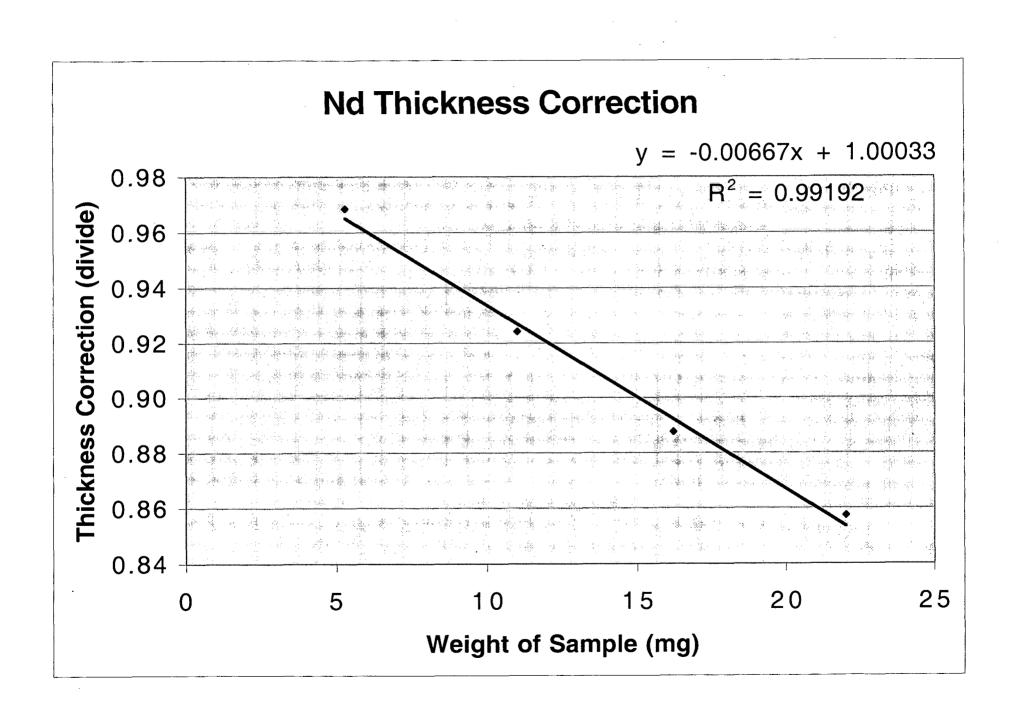
The Pm results were:

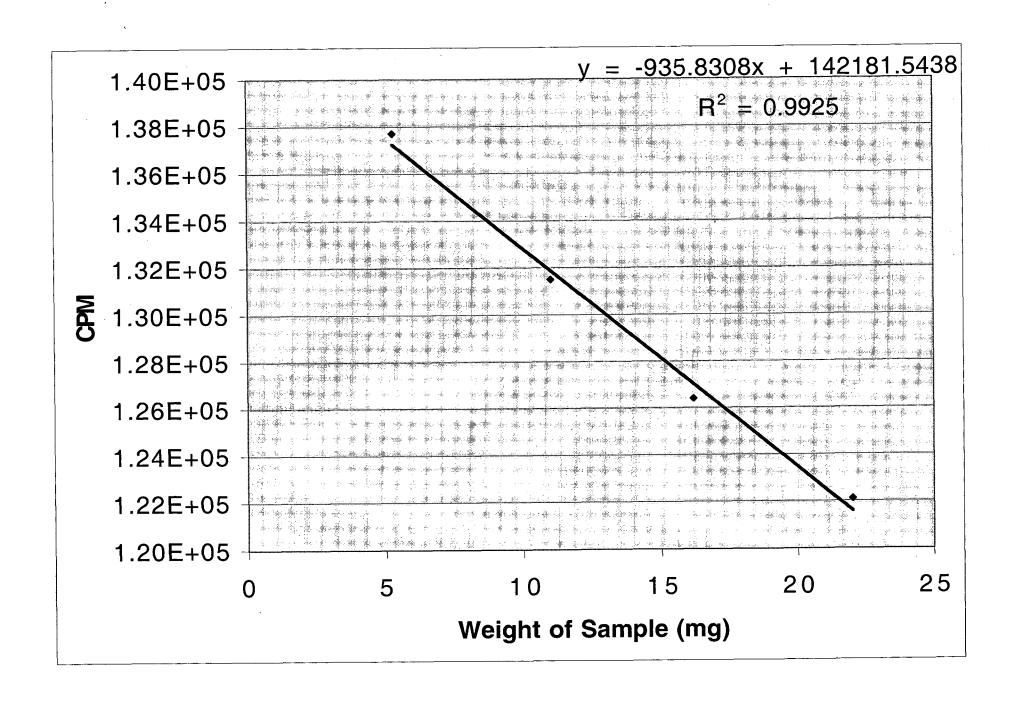
<u>Weight</u>	<u>Absorber</u>	Cpm at T	<u>Err</u>	Cpm at T	<u>Err</u>
<u>(mg)</u>		(CPM)	<u>%</u>	(CLSQ)	<u>%</u>
5.284	No	2.112E2	0.3	2.115E2	0.8
5.284	Yes	-	-	_	-

Attachment 1

5.284*	Yes	1.388E1	14.9	9.785	3.1
11.006	No	2.640E2	1.2	2.564E2	3.7
16.211	No	1.560E2	0.4	1.561E2	0.8
16.211	Yes	-	-	-	-
16.211*	Yes	7.184	7.5	7.774	3.8
22.024	No	1.949E2	1.9	1.877E2	4.0

^{*} Two component calculation





Attachment 2

Math A Us

Parent(1)-Daughter(2) Equilibrium:

Total Activity / Parent Activity

$$1) = \left[\lambda_1 n_1^{\circ} \left\{ \varepsilon_1 e^{-\lambda_1 \Delta t} + \left(\lambda_2 \varepsilon_2 / (\lambda_2 - \lambda_1)\right) \left(e^{-\lambda_1 \Delta t} - e^{-\lambda_2 \Delta t}\right) \right\} + \lambda_2 n_2^{\circ} \varepsilon_2 e^{-\lambda_2 \Delta t} \right] / \lambda_1 n_1^{\circ} \varepsilon_1 e^{-\lambda_1 \Delta t}$$

$$2) = e^{(\lambda 1 \Delta t)} \{ e^{-\lambda 1 \Delta t} + (\epsilon_2/\epsilon_1)(\lambda_2/(\lambda_2 - \lambda_1))(e^{-\lambda 1 \Delta t} - e^{-\lambda 2 \Delta t}) + (\lambda_2 n_2^{\ o} \epsilon_2/\lambda_1 n_1^{\ o} \epsilon_1)e^{-\lambda 2 \Delta t} \}$$

$$3) = 1 + (\epsilon_2/\epsilon_1)(\lambda_2/(\lambda_2-\lambda_1))(1 - e^{(\lambda_1-\lambda_2)\Delta t}) + (\lambda_2 n_2^{\ o}\epsilon_2/\lambda_1 n_1^{\ o}\epsilon_1)e^{(\lambda_1-\lambda_2)\Delta t}\}$$

For $\lambda_2 > \lambda_1$ and at $t \to \infty$ (equilibrium)

$$4) = 1 + (\varepsilon_2/\varepsilon_1)(\lambda_2/(\lambda_2-\lambda_1))$$

Linear Regression of Parent(1)-Daughter(2) Activity Curve:

Total (measured) Activity (for a perfect separation, $n_2^0 = 0$)

5) Total =
$$\lambda_1 n_1^{\circ} \{ \epsilon_1 e^{-\lambda_1 \Delta t} + (\lambda_2 \epsilon_2 / (\lambda_2 - \lambda_1)) (e^{-\lambda_1 \Delta t} - e^{-\lambda_2 \Delta t}) \} + \lambda_2 n_2^{\circ} \epsilon_2 e^{-\lambda_2 \Delta t}$$

Linearization

6) Total
$$(e^{\lambda 2\Delta t}) = \lambda_1 n_1^{\circ} \varepsilon_1 \{ e^{(\lambda 2 - \lambda 1)\Delta t} + (\varepsilon_2/\varepsilon_1)(\lambda_2/(\lambda_2 - \lambda_1))(e^{(\lambda 2 - \lambda 1)\Delta t} - 1) \} + \lambda_2 n_2^{\circ} \varepsilon_2$$

where the slope is $\lambda_1 n_1^{\circ} \epsilon_1$ and the intercept is $\lambda_2 n_2^{\circ} \epsilon_2$; and at equilibrium,

7) Total^o =
$$\{1 + (\varepsilon_2/\varepsilon_1)(\lambda_2/(\lambda_2-\lambda_1))\}\lambda_1 n_1^o \varepsilon_1$$

but a priori (ϵ_2/ϵ_1) is both a function of sample mass and is assumed to be unknown, therefore, define and effective efficiency for the counting, ϵ^* , so that,

8) Total^o =
$$\{1 + (\lambda_2/(\lambda_2 - \lambda_1))\}\lambda_1 n_1^o \epsilon^*$$

and,

9)
$$\{1 + (\lambda_2/(\lambda_2 - \lambda_1))\}\lambda_1 n_1^{\ o} \epsilon^* = \{1 + (\epsilon_2/\epsilon_1)(\lambda_2/(\lambda_2 - \lambda_1))\}\lambda_1 n_1^{\ o} \epsilon_1$$

10)
$$\varepsilon^* = \varepsilon_1 \{1 + (\varepsilon_2/\varepsilon_1)(\lambda_2/(\lambda_2-\lambda_1))\} / \{1 + (\lambda_2/(\lambda_2-\lambda_1))\}$$

11) Slope =
$$\lambda_1 n_1^{\circ} \epsilon^*$$

12) Intercept =
$$\lambda_2 n_2^{\circ} \epsilon_2 + \lambda_1 n_1^{\circ} (\epsilon_1 - \epsilon_2) (\lambda_2/(2\lambda_2 - \lambda_1))$$

Apply $K_T(\epsilon^*)$ or $K_1(\epsilon^*)$ to eqn 8 or eqn 11.